Negative polarity items and even

1 Polarity items

Some Negative Polarity Items (NPIs) from Ladusaw (1979):

- (1) a. * John has talked to *any* of the students.
 - b. ✓ John **hasn't** talked to *any* of the students.
- (2) a. * Someone has arrived *yet*.
 - b. \checkmark **No one** has arrived *yet*.
- (3) a. * Mary thinks that she has *ever* insulted anyone.
 - b. \checkmark Mary **doesn't** think that she has *ever* insulted anyone.

NPIs seem to be dependent on a *licensor*, which in the examples above is negation (in bold).

"[Negative-polarity-dependency] is a feature which must be associated with members of a wide variety of syntactic categories: determiners (*any*), sentence adverbs (*yet*, *ever*), verb phrases (*lift a finger*), intransitive verbs (*budge*), transitive verbs (*faze*), and perhaps, modals (*need*, *dare*) and particles (*either*)." Ladusaw (1979, p. 168)

There are also so-called *Positive Polarity Items* (PPIs; or in Ladusaw, *Affirmative Polarity Items*), but we won't worry about them here.

(4) *Someonelsomething* is a PPI:

I didn't read *something* for class.

a.	= There is something that I didn't read for class.	$\exists > not$
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- b. \neq It's false that [I read something for class]. not > \exists
- (5) The relative position of the licensor and NPI matter:
 - a. * Anything, I didn't read ____.
 - b. ** Anyone* **didn't** read the book.

Hypothesis 1: NPIs must be in the scope of negation.

This hypothesis is clearly wrong for many NPIs. For one, we would have to decompose licensors like *refuse* into *not agree*. But why not decompose *agree* into *not refuse*?

- (6) Ladusaw (1979, p. 102):
 - a. John **refused** to eat *any* of the bagels.

- b. * John agreed to eat *any* of the bagels.
- c. John **didn't** agree to eat *any* of the bagels.

Even more problematic is that NPIs are licensed in some constructions which do not obviously involve negation at all:

- (7) Chierchia (2013, p. 21):
 - a. * If you visit Sienna, you should *ever* try homemade ricciarellis.
 - b. If you *ever* try homemade ricciarellis, you will become addicted.
 - c. * Everyone who visited Sienna *ever* ate homemade ricciarellis.
 - d. Everyone who *ever* ate homemade ricciarellis became addicted.

Hypothesis 2: NPIs are licensed in *downward-entailing* (DE) environments (Ladusaw, 1979, following work by Gilles Fauconnier and Janet Fodor).

(8)	Upward-entailing:	(9)	Downward-entailing (DE):	
	Someone read (at least) one article		No one read (at least) one article	
	\Leftarrow Someone read (at least) two articles		\Rightarrow No one read (at least) two articles	
	\Leftarrow Someone read (at least) three art's		\Rightarrow No one read (at least) three articles	

Intuition: (Many) NPIs pick out the *lowest* point on a scale, which is the hardest to satisfy, and say, "even THAT point is true." (We will return to this intuition later.)

DE-ness is not a property of entire sentences. It is a property of functions of sets. Ladusaw gives the following general definition:

(10)
$$\delta$$
 is downward-entailing iff $\forall X \forall Y \left[X \subseteq Y \rightarrow \left[\delta(Y) \left\{ \begin{array}{c} \rightarrow \\ \subseteq \end{array} \right\} \delta(X) \right] \right]$

We can think of quantificational determiners (type $\langle \langle e, t \rangle, \langle \langle e, t \rangle, t \rangle \rangle$) as taking two set-type arguments, so we want to test them independently.

(11) "Subset" relations between predicates:

- λx_e . *x* is a good father
- $\supseteq \lambda x_e$. *x* is a father
- $\supseteq \lambda x_e$. *x* is a man...

(12) The restrictor of *every* is DE:

Every man is mortal.

- \Rightarrow Every father is mortal.
- \Rightarrow Every good father is mortal...

(13) The nuclear scope of *every* is not DE:

Everyone who applied for this program is a man.

- \Rightarrow Everyone who applied for this program is a father.
- ⇒ Everyone who applied for this program is a good father...

Hypothesis 2 predicts that NPIs are possible in the restrictor of *every* but not its scope (7c–d).

Exercise: Which of these quantifiers are DE in their restrictor (*A*)? In their scope (*B*)?

(14)	a.	a/some(A)(B) = 1	iff	$A\cap B\neq \emptyset$
	b.	no(A)(B) = 1	iff	$A\cap B=\emptyset$
	c.	exactly- $two(A)(B) = 1$	iff	$ A\cap B =2$
	d.	less-than-five(A)(B) = 1	iff	$ A\cap B <5$
	e.	at-least-five $(A)(B) = 1$	iff	$ A\cap B \geq 5$
	f.	not all(A)(B) = 1	iff	$A \setminus B \neq \emptyset$

We can also check DE-ness for other set-like types, like intensions ((s, t)):

(15) **"Subset" relations between intensions:**

 λw . I read at least one article in w

- $\supseteq \lambda w$. I read at least two articles in w
- $\supseteq \lambda w$. I read at least three articles in w...

(16) Conditional clauses are downward-entailing:

If I read at least one article, I will pass the class.

- \Rightarrow If I read at least two articles, I will pass the class.
- \Rightarrow If I read at least three articles, I will pass the class. ...

(17) The *consequent* clause of a conditional is not downward-entailing:

If Bill is a good student, he will read at least at least one article.

- \Rightarrow If Bill is a good student, he will read at least at least two articles.
- \Rightarrow If Bill is a good student, he will read at least at least three articles. ...

Hypothesis 2 predicts that NPIs are possible in conditional clauses but not in their consequent clauses (7a–b).

Negation is a common licensor, simply because it flips entailment relations and can create downward-entailing environments.

Strong NPIs:

Note that some NPIs (so-called strong NPIs) really require a licensing negation (Hypothesis 1) and DE-ness is insufficient. See for example English *in weeks*:

- (18) Chierchia (2013, p. 213–215):
 - a. * John saw Mary *in weeks*.
 - b. John didn't see Mary *in weeks*.
 - c. * If John has seen Mary *in weeks*, he will be upset.
 - d. * Less than five students have seen me *in weeks*.
 - e. * Every person who has seen Mary *in weeks* is upset with her.

2 Even

Another expression that cares about scales and entailment is *even*. (Fauconnier (1975) is credited with first making this connection between *even* and NPIs.)

Even, like *also* and *only*, is a focus-sensitive operator in English. Like *only*, it can appear as an adverb or attaching closer to the focus.

(19)	a. Alex even took the TURTLE to school.	adverb even	
	b. Alex took even the TURTLE to school. (=a)	constituent even	

- (20) Alex even took the turtle to SCHOOL. (\neq 19a,b)
- (21) Alex took the $[turtle]_F$ to school.

Prejacent proposition: Alex took the turtle to school.

Focused constituent: turtle

Alternatives to "turtle": frog, pig...

<u>Alternative propositions</u>: Alex took the *frog* to school, Alex took the *pig* to school...

even: the prejacent proposition "Alex took the turtle to school" was *less likely* than the alternative propositions, e.g. "Alex took the frog to school," "Alex took the pig to school"..., but the prejacent is nonetheless true.

(22) A basic definition for *even*:¹ $\begin{bmatrix} even & \alpha_t \end{bmatrix} = 1 \iff [\![\alpha]\!]^o = 1$ <u>Presupposition:</u> $\forall p \in [\![\alpha]\!]^f [p \neq [\![\alpha]\!]^o \rightarrow [\![\alpha]\!]^o <_{\text{likely }} p]$

How do we compute $p <_{likely} q$ for p and q of type t? We can do this using the intensions of p and q, of type (s, t).

¹*Even* might also introduce an *additive* presupposition, that one of the non-prejacent alternatives is true, just like *also*. But we'll ignore that here.

(23) **A more formal definition for** *even*:

$$\begin{bmatrix} & & \\ even & \alpha_{\langle s,t \rangle} \end{bmatrix}^w = 1 \iff \llbracket \alpha \rrbracket^o(w) = 1$$

$$\underline{Presupposition:} \forall p \in \llbracket \alpha \rrbracket^f \left[p \neq \llbracket \alpha \rrbracket^{o,w'} \rightarrow \left| \left\{ w'' : \llbracket \alpha \rrbracket^o(w'') \text{ true} \right\} \right| < |\{w''' : p(w''') \text{ true}\}| \right]$$

Here we measure "likelihood" by the number of worlds where each alternative is true.²



Exercise: Let's compute this.

3 Using *even* to explain negative polarity items

Notice that with minimizer NPIs, we can explicitly add an even (Heim, 1984):

- (25) a. * He lifted a finger.
 - b. He **didn't** (even) *lift a finger*.

Idea: (Some) NPIs are indefinites which have a requirement that they associate with a (possibly covert) *even* (Heim, 1984; Lee and Horn, 1994; Lahiri, 1998, a.o.).

(26)
$$\llbracket \text{read } any \text{ article} \rrbracket^{o} = \lambda x_{e} \cdot x \text{ read (at least) one article}$$

(27) $\llbracket \text{read } any \text{ article} \rrbracket^{f} = \begin{cases} \lambda x_{e} \cdot x \text{ read (at least) one article,} \\ \lambda x_{e} \cdot x \text{ read (at least) two articles,} \\ \lambda x_{e} \cdot x \text{ read (at least) three articles} \end{cases}$

²This treatment intuitively makes sense, but is non-standard, because it's not clear whether we can really count possible worlds, which may be infinite.



References

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